

Let's look at some common Natural Number Sequences.

### The Even Numbers

$$t = (2)(n)$$

start with  $n = 0$

$$\{0, 2, 4, 6, \dots\}$$

### The Odd Numbers

$$t = (2)(n) + 1$$

start with  $n = 0$

or

$$t = (2)(n) - 1$$

start with  $n = 0$

$$\{1, 3, 5, 7, \dots\}$$

### The Perfect Squares

$$t = n^2$$

$$\{0, 1, 4, 9, \dots\}$$

start with  $n = 0$

### The Perfect Cubes

$$t = n^3$$

$$\{0, 1, 8, 27, \dots\}$$

start with  $n = 0$

Let's focus on the two different rules given for the **Odd Numbers** and see how these rules generate the sequences.

$$t = (2)(n) + 1 \quad \text{starting with } n = 0$$

$n = 0$	$n = 1$	$n = 2$
$t = (2)(n) + 1$	$t = (2)(n) + 1$	$t = (2)(n) + 1$
$t = (2)(0) + 1$	$t = (2)(1) + 1$	$t = (2)(2) + 1$
$t = 1$	$t = 2 + 1$	$t = 4 + 1$
$r = 1$	$t = 3$	$t = 5$
	$r = 2$	$r = 3$

The sequence is **1, 3, 5, ...**; that is, the **Odd Numbers**.

$$t = (2)(n) - 1 \quad \text{starting with } n = 1$$

$n = 1$	$n = 2$	$n = 3$
$t = (2)(n) - 1$	$t = (2)(n) - 1$	$t = (2)(n) - 1$
$t = (2)(1) - 1$	$t = (2)(2) - 1$	$t = (2)(3) - 1$
$t = 2 - 1$	$t = 4 - 1$	$t = 6 - 1$
$t = 1$	$t = 3$	$t = 5$
$r = 1$	$r = 2$	$r = 3$

The sequence is **1, 3, 5, ...**; that is, the **Odd Numbers**.

Note how the starting value for  $n$  has an effect on the rule for  $t$ .

Also, note that for the rule  $t = (2)(n) - 1$  **starting with  $n = 1$** , the  $n$  and the  $r$  are the same for the whole sequence.

When this is the case, we can replace the  $n$  with  $r$  in the rule and write

$$t = 2r - 1$$

This allows us to find a term based on its rank in the sequence.